SOME ASPECTS ON CONTROL OF FUEL CELL HYBRID SOURCE AT THE FUEL CELL MAXIMUM POWER POINT UNDER DYNAMIC LOAD

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Abstract- In this paper is analyzed a fuel cell Hybrid Power Source (HPS) topology that can operate at maximum power point of fuel cell stack. The HPS power topology and its control are simulated in Matlab - Simulink® environment. The models for all used blocks are given and some control aspects are analyzed and discussed here.

Keywords: Hybrid Power Source, Maximum Power Point, Fuel Cell, Battery, Ultracapacitor, Modelling.

I. INTRODUCTION

As it is known, the fuel cell current dynamic must be limited in hybrid power source (HPS), especially when the Fuel Cell with Proton Exchange Membrane (PEMFC) is the main energy source of it. In the commercial PEMFC data sheet are mentioned some limitations for the level of PEMFC current regarding the ripple and slopes. These parameters are the main factors responsible for lower energy efficiency and reduced life cycle of PEMFC [1-6]. The level for the low frequency (LF) harmonics of PEMFC current set the PEMFC stack performances by hysteretic losses and more fuel consumption. Data sheet restrictions of the PEMFC ripple are specified on the frequencies bands and used in designing of the fuel cell HPS. The LF harmonics contributes with up to 10% reduction in the rated output power of PEMFC [7,8], so different solutions are proposed to mitigate of its [9-12]: increasing of the passive filter rated capacity, adding of active filters, implementing of an active control at the level of inverter system, using of interleaved converters, etc. For mono-phase inverter system powered by fuel cell HPS, the LF harmonics appear on high DC voltage bus at even multiples of twice of the grid frequency. For three-phase case, the LF harmonics appear at multiples of triple of grid frequency. These LF harmonics are propagated back through boost DC-DC converter on the HPS DC voltage bus. A HPS topology combines two or more energy sources and energy storage devices (ESD) that work together to supply the inverter system or store energy in ESD (such as stack of batteries and/or ultracapacitors) [13-16]. The HPS output port is a regulated DC voltage port [17]. The main control objective for the HPS vehicle applications is short respond to high energy demands [18-21]. When load require more power than is currently available from the PEMFC’s stack, the bidirectional converter drains energy from those ESD in order to make up the lack (see Figure 1 adapted from [21]).

For high energy efficiency, in fuel cell HPS the PEMFC stack must operates in the region close to maximum power point (MPP) at rated fuel flow [22-25]. The fuel flow level is changed by fuel cell current if ESD state of charge (SOC) is in the admissible range. The PEMFC stack ($P_{FCS}$) and ESD stack ($P_{ESD}$) assure the power flow on LV DC bus via the MPP boost converter ($P_1$) and bidirectional converter ($P_2$), respectively. The power balance is $P_{load} = P_1 + P_2$, and the power management is assures by the MPP controller and LV DC bus controller. The fuel cell MPP current ($I_{MPP}$) is tracked in an adaptive feedback loop by injecting the probing current [26, 27]. The power ripple becomes lowest when the operation point gets closer to MPP [28]. Also, using of ultracapacitors as ESD in fuel cell-based vehicles permits reduction of the hydrogen consumption and a reliable PEMFC operating under sharp power pulses [29, 30, 31].

In this paper, the modelling analysis will be focused on operating control of the fuel cell HPS at MPP of PEMFC stack. The remainder of the paper is organized as follows. The analyzed HPS topology is shown in Section 2. Section 3 presents the proposed modelling of fuel cell HPS topology in the Matlab-Simulink® environment.
Section 4 shows the appropriate control of both HPS controllers: hysteretic current controller and MPP tracking controller. Section 5 shown representative simulation results and last section concludes the paper.

II. ANALYZED FUEL CELL HPS TOPOLOGY

In Figure 2 is shown the HPS topology that will be analyzed in this paper. Note that ESD are directly connected to the LV DC bus. Consequently, the voltage on LV DC bus will have a slow variation in order to assure the balance of power flows when the MPP is changed. This choice does not affect the MPP tracking process. In this case the power balance is 

\[ P_{\text{load}} = P_1 + P_{\text{ESD}} \]

where 

\[ P_{\text{ESD}} = P_{\text{batt}} + P_{\text{Ucap}}. \]

The MPP boost converter is an appropriate solution to assure a low PEMFC current ripple. A hysteretic current controller is used to generate the switching command. The current error, \( I_{\text{MPP}} - I_{\text{PEMFC}} \), is used to turn the switch on and off, resulting in free-running operation.

III. MODELLING OF FUEL CELL HPS

In this section, the used models for PEMFC stack, ESD stack and boost converter are briefly explained.

A. Model of PEMFC Stack

Many improvements have been made to fuel cell model in recent years [33, 34, 35]. The variation of the PEMFC temperature (\( T \)) in time (\( t \)) depends by fuel cell current (\( I_{\text{FC}} \)) and can be calculated as:

\[
T = T_0 + (T_0 - T_0) + T_0 - I_{\text{FC}} \exp \left( \frac{-t}{t_{\text{H2}}} \right) \left( 1 - \exp \left( \frac{-t}{t_{\text{O2}}} \right) \right)
\]

where the parameters are mentioned in [36, 37]. The hydrogen partial pressure can be obtained with:

\[
H_{\text{H2}}(t) = V_{\text{tIFU}} \cdot N_{\text{Qst}} \cdot k_{\text{H2}} \cdot t_{\text{H2}}^2
\]

where:
- \( t_{\text{H2}} \) is hydrogen time constant (s);
- \( V_{\text{tIFU}} \)- Volume of the cathode (m3);
- \( N_{\text{Qst}} \)- Oxygen input flow (kmol s\(^{-1}\) or l/min);
- \( k_{\text{H2}} \)- Oxygen valve molar constant [kmol (atm s\(^{-1}\)];

Usually, the hydrogen and oxygen input flows are inputs for PEMFC model. The fuel flow rate is chosen as input parameter in this paper.
Figure 4. Analyzed fuel cell HPS topology (adapted from [21])

The Nernst’s voltage is implemented as:

$$E_{\text{Nerst}} = 1.229 - 8.5 \cdot 10^{-4} \cdot (T - 298) + 4.308 \cdot 10^{-5} \cdot T \cdot \ln \left( \frac{P_{\text{H}_2} + P_{\text{O}_2}}{2} \right)$$  \hspace{1cm} (4)

The activation voltage loss can be written as:

$$E_{\text{act}} = \xi_1 + \xi_2 \cdot T + \xi_3 \cdot T \cdot \ln(I_{\text{FC}}) + \xi_4 \cdot \ln(C_{\text{O}_2})$$  \hspace{1cm} (5)

where $C_{\text{O}_2}$ represents the dissolved oxygen concentration in the interface of the cathode catalyst and the $\xi_i$ parameters, $i=1-4$, are mentioned in references [33, 35, 36].

The ohmic voltage loss is implemented as:

$$E_{\text{ohmic}} = J_{\text{FC}} \cdot R_{\text{ohmic}}$$  \hspace{1cm} (7)

where:

- $J_{\text{FC}}$ - Current density (A/cm$^2$);
- $R_{\text{ohmic}}$ - Equivalent membrane resistance ($\Omega$);
- $R_m$ - Contact resistance between membrane and electrodes ($\Omega$);
- $tm$ - membrane thickness [cm];
- $A$ - Activation area (cm$^2$);
- $r_m$ - Resistivity of Nafion membrane ($\Omega$cm$^2$m$^{-1}$):

$$r_m = \frac{0.0634 + 3 \cdot J_{\text{FC}}}{\exp(4.18 \cdot (T - 303) / T)}$$  \hspace{1cm} (8)

where $\lambda_m$ represent the water content of the membrane and it is a input of PEMFC model set to 2.

The concentration voltage loss is implemented in the subsystem 5 and can be written as:

$$V_{\text{conc}} = B \cdot \ln \left( 1 - \frac{J_{\text{FC}}}{J_{\text{max}}} \right)$$  \hspace{1cm} (9)

where $B$ is a modeling constant (V) and $J_{\text{max}}$ represents the maximum current density (A/cm$^2$).

The PEMFC output voltage can be calculated as:

$$V_{\text{FC}} = N \cdot (E_{\text{Nerst}} \cdot E_{\text{ohmic}} \cdot V_d)$$  \hspace{1cm} (10)

where $V_d$ is voltage over $R_d$ resistance and $R_d$ is equivalent resistance representing the sum of activation and concentration resistances:

$$R_d = \frac{V_d}{I_{\text{FC}}} \cdot E_{\text{act}} + E_{\text{conc}}$$  \hspace{1cm} (11)

The PEMFC dynamic related to the $R_d$ resistance in parallel with double layer capacitor ($C$) is implemented as:

$$I_{\text{FC}} = \frac{V_d}{R_d} + C \cdot \frac{dV_d}{dt} \Rightarrow V_d = \frac{I_{\text{FC}} \cdot R_d}{I_{\text{FC}} \cdot s + 1}$$  \hspace{1cm} (12)

where $I_{\text{FC}}=C \cdot R_d$ represents the fuel cell time constant.

B. Model of Mixed ESD Stack

The used battery model in this paper is well known [38]. The exponential zone dynamics is modeled by:

$$E_{\text{ex}}(q) = A \cdot \exp(-B \cdot q)$$  \hspace{1cm} (13)

where:

- $q=I_{\text{batt}} \cdot t$ is current battery capacity (Ah);
- $I_{\text{batt}}$ - Battery current (A);
- $A$ - Exponential voltage (V);
- $B$ - Exponential capacity (Ah)$^{-1}$.

Battery operating mode is modeled by $S$ signal, which is the output of a comparison block that compare the low-pass filtered battery current, $i_{LPFbatt}$, with zero reference. Consequently, $S = 0$ during battery discharge ($i_{LPFbatt}>0$) and $S = 1$ during battery charging ($i_{LPFbatt}<0$). Finally, the battery voltage, $E_{\text{Batt}}$, is given by charge ($f_c$) or discharge ($f_d$) function as:

$$E_{\text{Batt}} = E_w + K_r \cdot i_{LPFbatt} + K_t \cdot \frac{q + E_{\text{ex}}}{q + 10} + K_r \cdot \frac{q + E_{\text{ex}}}{q + 10}$$  \hspace{1cm} (14)

where:

- $E_w$ is a constant – the working battery voltage (V);
- $K_r$ = Polarization constant V/(Ah);
- $K_t$ = Polarization resistance ($\Omega$);
- $i_{LPFbatt}$ = Low frequency battery current dynamics (A);
- $Q$ = Maximum battery capacity (Ah).

Battery state of charge, $SOC_{\text{batt}}$, is computed as:
\[ \text{SOC}_{\text{batt}} = 100 \left( 1 - \int_{t_0}^{t} \frac{Q_{\text{batt}}(t)}{Q} \, dt \right) \]  (15)

The parameters for used 160V/38Ah battery are:

- \( A = 15 \text{V} \)
- \( B = 0.375 \text{Ah}^{-1} \)
- \( K_c = 0.03 \text{V/(Ah)} \)
- \( K_r = 0.03 \text{Ω} \)
- \( E_w = 163 \text{V} \)
- \( Q = 43 \text{Ah} \)

\( R_{\text{batt}} \) is set of 0.04 \( \text{Ω} \) and the battery output voltage, \( V_{\text{batt}} \), is computed as:

\[ V_{\text{batt}} = E_{\text{batt}} - R_{\text{batt}} \cdot i_{\text{batt}} \]  (16)

For the used 100F/160V ultracapacitors stack is used a first order model [35, 36] with the series, \( R_{s} \), and parallel, \( R_{p} \), resistances set at 0.01 \( \text{Ω} \) and 1 k\( \text{Ω} \), respectively.

C. Model of Boost Converter

The boost converter model is well known, so only the used parameters are given below. In on-state both IGBT and FW-Diode models have a \( R_{\text{on}} \) internal resistance and a \( L_{\text{on}} \) inductance of 0.01\( \text{Ω} \) and 1\( \mu \text{H} \), respectively, but the forward voltage, \( V_f \), is set different to 1V and 0.8V, respectively. Also, the fall time, \( T_f \), and tail time, \( T_t \), is set different to 1\( \mu \text{s} \) and 2\( \mu \text{s} \), respectively. Both IGBT and FW-Diode models use a series RC snubber circuit with \( C_{\text{snubber}} = 0.1\mu \text{H} \) and \( R_{\text{snubber}} = 100 \text{Ω} \). The boost inductance, \( L_{\text{boost}} \), is set to 10mH value and its series resistance, \( r_L \), at 10m\( \Omega \).

IV. CONTROL OF FUEL CELL HPS

In this section, the HPS control is analyzed and briefly explained.

A. Hysteric Current Controller

Switching command for boost converter is obtained using a hysteric current controller (see Figure 5). The input current is the difference between the fuel cell current, \( i_{\text{FC}} \), and the current output of the MPP tracking controller that estimate the MPP fuel cell current in an adaptive loop (see Figure 6).

The operating relationships of boost converter are

\[ v_{\text{FC}} = (r_L + R_{\text{on}}) \cdot i_{\text{FC}} + (L_{\text{boost}} + L_{\text{on}}) \frac{di_{\text{FC}}}{dt} + V_f \]

\[ v_{\text{FC}} = (r_L + R_{\text{on}}) \cdot i_{\text{FC}} + (L_{\text{boost}} + L_{\text{on}}) \frac{di_{\text{FC}}}{dt} + V_f + v_{L_{\text{Vbus}}} \]  (17)

for IGBT on-state and FW-Diode on-state, respectively.

For example, at rated load and fuel cells stack operating at MPP (\( V_{\text{FC}} = V_{\text{MPP}} = 26.6 \text{V} \), \( I_{\text{FC}} = I_{\text{MPP}} = 45 \text{A} \)) with a ripple factor of fuel cell current of about \( R_{\text{FC}} = 5\% \), if \( V_{L_{\text{Vbus}}} = 100 \text{V} \), \( L_{\text{boost}} = 10 \text{mH} \), and neglecting the resistive effect in relationships (11), then switching period is \( T \approx 1 \text{kHz} \) (see relation 18):

\[ T \approx (L_{\text{boost}} + L_{\text{on}}) \cdot R_{\text{FC}} \cdot I_{\text{MPP}} \left( \frac{1}{V_{\text{MPP}}} + rac{1}{V_{L_{\text{Vbus}}}} \right) \]  (18)

B. MPP Tracking Controller

The adaptive MPP feedback loop using a high-pass filter is explained in [26]. The advantages of using a band-pass filter centred on the sine frequency are shown in [39, 40]. After normalization of PEMFC power, \( P_{\text{FC}} \) with \( k \) gain (=1/Area), the probing power signal is filtered and demodulated by multiplication with 1 Hz sine dither. After that, it is integrated and amplified by \( k_1 \) gain and, finally, is superimposed on it the amplified dither (\( k_2 \sin \omega t \)) (Figure 5). Some power spectrums are shown in next section. It is shown that only first three harmonics of probing power signal are important in the MPP tracking.

V. SIMULATION RESULTS

The time for MMP tracking is around of hundreds of seconds when the start current is zero (Figure 3). In Figure 7 and 8 are shown the process of MPP tracking when the PEMFC operation (close of MMP) is perturbed by a pulse in the fuel flow rate (that gives \( \Delta P \approx 500 \text{W} \)). It can be observed that the time for MMP tracking is less of ten second. The PEMFC behaviour in the tracking of the MMP sequence shown in Figure 3 is presented in Figure 9. Without the bidirectional converter and its controller (see Figures 1 and 2), the voltage on the LV DC bus, \( V_{L_{\text{Vbus}}} \) is around the ESD nominal voltage value to assure the power balance (see Figure 10).
VI. CONCLUSIONS

In this paper, the control objective for the fuel cell HPS is to operate at the MPP of PEMFC for any dynamic of load. The proposed HPS architecture was modelled in Matlab–Simulink® environment. The simulation results have successfully shown that this operation of HPS is possible by using an adaptive MPP tracking control. The power balance is assured by the ESD stack.

REFERENCES


BIOGRAPHY
Nicu Bizon was born in Albesti Muscel, Romania, on February 14, 1961. He received a five-year degree in electronic engineering from the University “Polytechnic” of Bucharest, Romania, in 1986 and the Ph.D. degree in Automatic Systems and Control from the same university, in 1996. He is currently a Professor with the University of Pitesti, Romania. Previously, he was in hardware design with Dacia Renault SA, Romania. He has authored of six books in Power Converter area, one in Theory and Control Systems, one in Fuzzy Control, one in Hardware topologies for PC and Devices, and one in Medical Electronics and Informatics (all in Romanian language). Also, he is co-author of the book Fundamentals of Electromagnetic Compatibility, Theory and Practice (in English language) and of a book chapter - “Intelligent control of the Energy Generation System”, in the book “Intelligent Information Systems and Knowledge Management for Energy: Applications for Decision Support, Usage and Environmental Protection”. His current research interests include the broad area of nonlinear systems, on both dynamics and control, and power electronics. He has authored or coauthored of several papers (over to 100) in journals (ISI/INSPEC or Romanian Academy indexed) and international conference proceedings. He is an Associate Editor of the Journal of the University of Pitesti “Electronics and Computer Science” and program chair and proceeding Editor of the Int. Conference on “Electronics, Computers and Artificial Intelligence - ECAI”, 2005, 2007 and 2009 editions.